Contingent Preferences and the Sure-Thing Principle: 
Revisiting Classic Anomalies in the Laboratory*

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Abstract

We formalize an aspect of hypothetical thinking first pointed out by Savage–who referred to it informally as the sure-thing principle (STP)–and show that it underlies many of the classic anomalies in decision and game theory. We perform an experimental test of STP and find that indeed some of the most common anomalies found in the laboratory, including overbidding in auctions, naive voting in elections, and both Ellsberg and Allais types of paradoxes can in large part be attributed to the failure of the type of hypothetical thinking underlying STP.

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1 Introduction

Hypothetical or contingent thinking is a form of “what–if” thinking that entails reasoning about events without knowing whether or not these events are true or will occur. A large literature in psychology finds that people have difficulty with various forms of hypothetical thinking.\textsuperscript{1} Given the role of hypothetical reasoning in explaining anomalies in psychology, it seems plausible that it has a role in producing anomalies in economics, where hypothetical thinking remains relatively unexplored. The economics literature has focused on several other interesting mechanisms to explain anomalies. Some of these mechanisms include mistakes with Bayesian updating, failure to understand that other people’s actions convey useful information, violations of axioms with normative appeal (such as the independence axiom), and preference-based explanations including risk, regret, and ambiguity aversion.

In this paper, we show that subjects in the laboratory have trouble with a very particular form of hypothetical thinking. More importantly, we find that difficulty with this particular form of hypothetical thinking underlies a large part of the mistakes and anomalies uncovered in several classic economic environments. In particular, we provide a unifying explanation for behavior documented in two very different strands of the literature. One strand shows that people make systematic mistakes, particularly in strategic settings. Examples include the winner’s curse in common value auctions, overbidding in second-price private-value auctions, and non-pivotal voting in elections. The second strand of the literature documents violations of expected utility axioms, such as the Ellsberg and Allais paradoxes.

The particular type of hypothetical thinking underlying the standard anomalies is what Savage (1972) informally referred to as the sure-thing principle (STP). Savage gave the following example to illustrate the principle. A businessman has to decide whether or not to buy a property. The businessman considers the outcome of the next presidential election relevant for this decision. He asks himself if he would prefer to buy the property in the hypothetical case that the Republican candidate were to win, and decides that he would do so. Similarly, he would also prefer to buy the property if the Democratic candidate were the winner. Since the businessman prefers to buy under either event, STP then requires that he prefers to buy the property.

The type of hypothetical thinking embodied by STP not only underlies the classic examples from decision theory, such as the Ellsberg and Allais paradoxes, but also examples from game theory. Consider, for example, a typical common-value election where, if a voter knew she was pivotal, then she would vote against her private information. In the event she is not pivotal, then her vote is irrelevant and so she should be indifferent. Thus, STP requires the voter, who has no information about her pivotal status, to vote against her private information. But a naive voter who does not understand pivotality may violate STP by actually voting according to her private information.

We use Savage’s framework as a convenient language to formalize STP and its connections to Savage’s postulates. We then test the extent to which STP fails and the extent to which such failures are responsible for the typical reversals or anomalies often attributed to various causes in the decision and game theory literatures.

We study five problems: Ellsberg, common-consequence and common-ratio Allais, a common-value election, and a second-price private-values auction. Our research strategy is to run subjects through standard versions of each of these canonical problems (we call these noncontingent versions of these problems). We then run subjects through slight alterations of each problem, removing the need for subjects to employ the type of hypothetical sophistication captured by STP (we call these variations contingent versions of the problems).

We find relatively large rates of failure of STP in all problems that we study. In particular, we report a rate of violations of STP that ranges from 20% to 70% across all problems. We also emphasize the importance of controlling for STP in order to investigate the extent of violations of standard postulates, such as Savage’s P2 (which we refer to as separability) and dominance. For example, violations of separability could possibly go up, down, or remain the same when controlling for subjects’ difficulty with contingent thinking. Consistent with the literature, we find violations of separability or dominance in all the problems that we study. But we find that, when controlling for failure of STP using the contingent treatment, these violations drop by half in all problems except the common-consequence Allais problem. Thus, a large part of the anomalies are driven by the failure of the particular form of hypothetical thinking formalized via STP.

Our results have several implications. The first implication is that, despite the fact that strategic and decision problems are usually studied from different perspec-
tives, there is actually common ground between them in the form of a particular form of hypothetical thinking. The second is that our subjects are not good at thinking through the state space in the way modelers often assume, and there is indeed a very specific way in which this phenomenon can be formalized and tested. A third implication speaks to welfare analysis. As the literature points out, it is reasonable that, for example, overbidding in auctions can be attributed to a preference for winning and that the Ellsberg paradox can be attributed to ambiguity aversion. From a welfare perspective, however, the question is the extent to which such behavior constitutes preferences or mistakes. While this is a difficult question to answer, the finding that overbidding and Ellsberg-type anomalies decrease by one-half in the contingent treatment suggests that difficulty with hypothetical thinking also plays an important role. Fourth, the finding that anomalies decrease in the contingent treatment suggests that there is room for interventions that help people think hypothetically and be more consistent with postulates with normative appeal, such as dominance.

Finally, the literature has previously acknowledged that we often make the implicit assumption that the agent can construct the state space in the same way as the modeler, while in fact incomplete preferences or anomalies may precisely stem from the fact that states are not naturally given and may be hard to construct (e.g., Gilboa et al., 2009). Our finding that subjects have trouble with hypothetical thinking suggests that we should pay more attention to theories of decision-making that do not rely on hypothetical thinking, such as case-based decision theory (Gilboa and Schmeidler, 1995) or the notion of obviously dominant strategies in games (Li, 2016).

The importance of hypothetical or contingent thinking has been recognized in several economic environments (see, e.g., Shafir and Tversky (1992) in the context of the prisoner’s dilemma, Charness and Levin (2009) in environments with adverse selection, Dal Bó et al. (2016) in settings where subjects fail to fully anticipate the equilibrium effects of new policies, and Ngangoue and Weizsäcker (2017) in a market setting where price reveals information). Li (2016) formally introduces the notion of an obviously dominant strategy as a strategy that a cognitively challenged player who cannot perform a certain kind of contingent thinking can recognize as dominant. He shows in an experiment that subjects play obviously dominant strategies at much higher rates than non-obviously dominant ones. Zhang and Levin (2017) model the case of a player who can recognize dominant strategies within partitions of the state-space and propose the notion of a partition dominant strategy, which includes
obviously dominant strategy as a special case. They provide experimental evidence that the notion can help design mechanisms that increase play of dominant strategies. In an earlier paper (Esponda and Vespa, 2014), we distinguished between information extraction and hypothetical thinking in a voting context, but did not formalize the notion of hypothetical thinking. Moreover, that paper was closer to the literature on dynamic choice; its main goal was to compare behavior in the noncontingent treatment with behavior in a *sequential* treatment where, unlike the experiments in this paper, the subject was informed about the relevant event before making a decision.

The potential difference between the noncontingent and contingent treatments has been pointed out by previous literature in the specific context of the common-ratio Allais paradox. Tversky and Kahneman (1981) and Holler (1983) find significant differences between treatments. In a detailed analysis of the common-ratio Allais paradox, Cubitt et al. (1998) decompose the paradox into four principles of dynamic choice and then test these principles in the lab. One of these tests is a comparison between the noncontingent and contingent treatments. They find no significant differences in the marginal responses across treatments, like we do for this specific problem. Their focus, however, is different than ours and so they do not test if there is a reduction of reversals when both questions of the Allais paradox are asked using the standard (i.e., noncontingent) treatment (we find there is). To our knowledge, however, there has been no formalization of the form of hypothetical thinking that underlies this phenomenon nor any experimental work finding a common source linking mistakes in strategic environments such as auctions and elections with the classic anomalies in decision problems.\(^2\)

There is a large experimental literature for each of the anomalies that we focus on. See, for example, Bazerman and Samuelson (1983), the survey by Kagel and Levin (2002), Charness and Levin (2009), Ivanov et al. (2010), Esponda and Vespa (2014), and Levin et al. (2016) for mistakes in common value settings, such as auctions or elections;\(^3\) Kagel et al. (1987), Kagel and Levin (1993), and Harstad (2000) for overbidding in second-price private value auctions; and MacCrimmon and Larsson (1979), the survey by Camerer (1995), Wakker (2001), Halevy (2007), Andreoni et

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\(^2\)In a theory paper, Eliaz et al. (2006) make a connection between anomalies in decision and game theory environments by establishing a formal equivalence between violations of expected utility theory and choice shifts in groups.

\(^3\)See also the experimental literature on correlation neglect, e.g., Eyster and Weizsäcker (2010) and Enke and Zimmermann (2013).
al. (2014), Dean and Ortoleva (2015), and Kovářík et al. (2016) for a limited sample of the very large literature on the Ellsberg (1961) and Allais (1953) paradoxes. This experimental literature has also motivated a large theoretical literature for modeling the behavior of agents who make mistakes or have richer types of preferences.\(^4\)

It is important to emphasize that our main finding that failure of STP underlies all of these anomalies does not take any merit away from the interesting mechanisms uncovered by previous work. In fact, the mechanisms examined in the literature (e.g., overbidding, ambiguity aversion, etc.) can be thought of as some of the factors that cause STP to fail in these problems. The reason why these problems have not been connected before is likely to be that the mechanisms are all very different. What we find in this paper is that there is indeed large common ground between these seemingly dissimilar settings, in the form of failure of a particular form of hypothetical thinking, as embodied by STP.

In Section 2, we use an example from decision theory and an example from game theory to illustrate the theoretical framework that underlies our experimental design. We formally introduce the theoretical framework in Section 3, describe the experimental design in Section 4, and present the experimental results in Section 5. We conclude in Section 6.

## 2 Illustrative examples

**ILLUSTRATIVE EXAMPLE 1: SECOND-PRICE AUCTION.** Consider a decision maker who participates in an auction where the highest bid wins and pays the bid of the second-highest bidder. There is one other bidder in this auction who is known to bid $0.50, $4.50, or $8.50 with equal probability. The decision maker must choose an integer bid from $1 to $8. The decision maker gets $5.50 if she wins the auction and an outside value of $3 if she does not.\(^5\)

We use Savage’s standard framework of decision-making under uncertainty to

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\(^4\)For theoretical responses to mistakes, see Eyster and Rabin (2005), Crawford and Iriberri (2007), Jehiel and Koessler (2008), and Espouda (2008). For theoretical responses to the paradoxes, see the surveys by Machina (2008), Gilboa and Marinacci (2011) and Machina and Siniscalchi (2013). For a critical assessment of the ambiguity aversion literature, see Al-Najjar and Weinstein (2009) and Siniscalchi (2009).

\(^5\)While it is standard to normalize the outside to be zero, here we illustrate the ideas using the payoffs from the actual experiment, where an outside value of $3 guarantees that subjects do not incur losses.
illustrate this problem in Table 1. There are three states of the world, corresponding to the three possible bids of the competitor, and the auction problem is represented by Question 1, where the decision maker chooses one of two acts. Act $f'$ corresponds to a bid of $1, $2, $3, or $4 while act $g'$ corresponds to a bid of $5, $6, $7, or $8. We also include a Question* that contrasts two constant acts, $f$ and $g$, that deliver payoffs of $3 and $1, respectively. We will not ask Question* in the experiment but will rather simply assume that more money is preferred to less, i.e., $f$ is preferred to $g$.

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<thead>
<tr>
<th>Question*</th>
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<th>$A^c$</th>
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<tr>
<td>$f$</td>
<td>4.5</td>
<td>0.5</td>
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<tr>
<td>$g$</td>
<td>8.5</td>
<td>5.0</td>
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<tr>
<th>Question 1</th>
<th>$f'$</th>
<th>$g'$</th>
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<tr>
<td>$f'$</td>
<td>4.5</td>
<td>3.0</td>
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<tr>
<td>$g'$</td>
<td>8.5</td>
<td>1.0</td>
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Table 1: Auction problem

In the auction, the choice of an integer bid from $1 to $8 is only relevant in the event that the other bidder bids $4.50. In this case, however, it is optimal to lose the auction by submitting a bid of $1, $2, $3 or $4, which is represented by $f'$. The paradox in this problem is that, in a treatment where subjects in the role of the decision maker are asked to submit an integer bid from $1 to $8, a significant fraction of subjects end up overbidding and choose $g'$ over $f'$. Note that, under the assumption that $f$ is preferred to $g$ in Question*, which is the assumption that more money is preferred to less money, then this choice constitutes a reversal: $f$ is preferred to $g$ but $g'$ is preferred to $f'$. This reversal is a violation of a crucial postulate in Savage’s framework that we refer to as dominance (henceforth abbreviated by DOM). We refer to this benchmark treatment as the noncontingent treatment.

Consider next a different treatment, which we call the contingent treatment, where we describe the same problem in a slightly different way. We now tell the subject that she will get $5 if the other bidder bids $0.50 and she will get $3 if the other bidder bids $8.50. If, however, the other bidder bids $4.50, then the subject has to choose an integer bid from $1 to $8. Crucially, we ask the subject to commit to a choice in case event $A = \{4.50\}$ is realized before she knows whether or not event $A$ is realized. Thus, the subject faces the same choice between $f'$ and $g'$ that is faced by a subject
in the noncontingent treatment. (In particular, the subject also faces a static choice problem in the contingent treatment; for a discussion of a dynamic choice problem where the subject is asked to move after receiving information about an event, see Section 4.2.)

According to standard theory, a subject’s choice between $f'$ and $g'$ should not depend on whether she faces the noncontingent or contingent version of the question. But, in practice, one can imagine that the contingent treatment helps the subject to focus on the event $A$ where the consequences differ. In other words, it is possible that the contingent treatment facilitates hypothetical thinking.

We argue that there are two underlying principles behind the failure of dominance (DOM). The first is a contingent version of DOM. In particular, if the subject continues to choose $g'$ in the contingent treatment, then we say that a contingent version of dominance, which we call C-DOM, is violated.

The second principle, and the main focus of the paper, is what we refer to as the sure-thing principle and abbreviate by STP. In the example of Table 1, STP says that if $f'$ is preferred to $g'$ contingent on event $A$ and $f'$ is indifferent to $g'$ in its complement, $A^c$, then $f'$ must be preferred to $g'$ in the noncontingent treatment. In particular, by comparing questions across treatments, we can assess the extent to which STP fails in our setting. In this example, an agent would violate STP if she were to prefer different alternatives across treatments. Figure 2 illustrates the connection between the questions and postulates for this example.

**ILLUSTRATIVE EXAMPLE 2: ELLSBERG.** Consider Ellsberg’s (1961) one-urn problem, where there is an urn with 90 balls, 30 of which are red and 60 of which are yellow or blue. The problem is depicted in Table 2, where there are 3 states of the world, $red$, $yellow$, and $blue$. A decision maker faces choices between four acts, $f$, $g$, $f'$, and $g'$, where each act maps the states of the world into monetary rewards.
Table 2: Example - Ellsberg problem

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<thead>
<tr>
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<th>( A )</th>
<th>( A^c )</th>
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| \( red \)    | \( f \) | \$10 \$
| \( yellow \) | \( g \) | \$0 \$
| \( blue \)   | \( f' \) | \$10 \$
|               | \( g' \) | \$0 \$

In the standard experiment in the literature, which corresponds to what we call the *noncontingent treatment* in this paper, a subject is asked two questions. For each question, a ball is drawn from the urn with replacement, and the subject must make a choice before knowing the color of the drawn ball. In Question 1, the subject must choose between two acts, \( f \) (win if red or blue) and \( g \) (win if yellow or blue). In Question 2, the subject is asked to choose between two other acts, \( f' \) (win if red) and \( g' \) (win if yellow). A typical response pattern is to prefer \( g \) in the first question and \( f' \) in the second question. These choices are consistent with an aversion to ambiguity, because in each case the subject chooses the alternative with the known probability of success (2/3 in the first question and 1/3 in the second question). As is well known, these choices constitute a reversal and, therefore, violate one of Savage’s central postulates, which he called P2 and we refer to in this paper as separability and abbreviate by SEP.

Consider next a different treatment, which we call the *contingent treatment*, where we ask the same questions in a slightly different way. For the first question, we tell a subject that, if the ball is \( blue \), then she will get \$10. And, if the ball is \( red \) or \( yellow \), then she has a choice between an option that pays \$10 if the ball is red and an option that pays \$10 if it is yellow. Crucially, we ask the subject to commit to a choice in case event \( A = \{ red, yellow \} \) is realized before she knows whether or not the state will be in \( A \). Thus, the subject faces the same choice between \( f \) and \( g \) that is faced by a subject in the first question of the noncontingent treatment. For the second question, we proceed in the same way except that we tell the subject that she will get \$0 if the ball is \( blue \). Thus, the subject faces the same choice between \( f' \) and \( g' \) that is faced by a subject in the second question of the noncontingent treatment.

Once again, according to standard theory, for each question, a subject should give the same answer whether she is asked the noncontingent or contingent version of
the question. But, in practice, one can imagine that the contingent treatment helps subjects focus on the event $A$ where the consequences differ.

We argue that there are two underlying principles behind the failure of Savage’s separability postulate (SEP). The first is a contingent version of SEP. For example, if the subject continues to choose $g$ and $f'$ in the contingent treatment, then we say that a contingent version of separability, which we call C-SEP, is violated.

The second principle, which is the principle that, as we emphasize, underlies problems from both decision and game theory is, once again, Savage’s STP. In the example of Table 2, STP says that if $f$ is preferred to $g$ contingent on event $A$ and $f$ is indifferent to $g$ in its complement, $A^c$, then $f$ must be preferred to $g$ in the noncontingent treatment. The same is true regarding Question 2 between $f'$ and $g'$. In particular, by comparing questions across treatments, we can assess the extent to which STP fails in our setting. In this example, an agent would violate STP if she were to prefer different alternatives across treatments for either Question 1 or 2. Figure 2 illustrates the connection between the questions and postulates for this example.

THEORETICAL FRAMEWORK. We use Savage’s framework as a convenient language to formalize the specific type of hypothetical thinking that underlies the anomalies that we study. Savage does not give a formal definition for STP, but rather uses this principle as motivation for two of his central postulates, P2 and P3.\(^6\) For this reason, sometimes the literature conveniently refers to P2 (which we call SEP in this paper) as the sure-thing principle, although we keep the names different in order to emphasize that these are different concepts.

\(^6\)Savage explicitly acknowledges this point by writing that “It will be preferable to regard the [sure-thing] principle as a loose one that suggests certain formal postulates...” (pg. 22).
Savage derives from the original, primitive preference relation what he calls a conditional preference relation. In the businessman example, there is a derived preference relation conditional on the event that a Republican wins and another one conditional on the Democrat winning. In fact, if the original preference relation satisfies SEP, then Savage's derived conditional preference relation must satisfy what he had informally referred to as STP. Savage (1972) formally states this result in Theorem 2, pg. 24, although he never explicitly refers to it as a formalization of STP.

Our key point of departure is that we consider both the original and conditional preference relations to be primitives. The reason is that, in principle, the conditional preference relation constitutes a different conceptual object and it may be inconsistent with the original one. To avoid confusion with Savage's definition, we refer to our new, conditional primitive as a contingent preference relation. We then formally define STP as a consistency requirement between the original and the contingent preference relations that captures the contingent reasoning behind the auction and Ellsberg examples discussed above, Savage's businessman story and the voting example discussed in the introduction, and several other contexts, as we illustrate in the paper.

It is well known that postulates P2 and P3 are central to Savage's theory of subjective expected utility; in addition, early examples by Allais (1953) and Ellsberg (1961) illustrate violations of P2 (recall that we refer to P2 as SEP in this paper). A bit less obvious, it is also the case that a common-ratio version of the Allais paradox, the voting paradox described above, and overbidding in a second-price auction, all violate a postulate that is implied by both P2 and P3 and that we refer to in this paper as dominance (DOM).

In the next section, we show that what we formally define as STP underlies classic anomalies from both decision and game theory experiments. To be more precise, we define corresponding versions of SEP and DOM, which hold on Savage's original preference relation, on our contingent preference relation. We call these postulates C-SEP and C-DOM. We then formally show that, if STP and C-SEP (or C-DOM) hold, then SEP (or DOM) must also hold for the original preference relation, provided that a simple indifference postulate is satisfied, which we call C-REF, for reflexivity. This result formalizes the claim that a very particular form of hypothetical thinking, modeled via our definition of STP, underlies behavior in classical environments from both decision and game theory. We then apply the framework to test to what extent
STP fails in the classic problems, compared to C-DOM or C-SEP.\textsuperscript{7}

3 Theoretical framework

Hypothetical thinking is relevant in many settings but is nevertheless an elusive concept in the sense that it can be challenging to formalize. We will use the framework introduced by Savage as a convenient language to formalize the specific type of hypothetical thinking that underlies the anomalies that we study. One advantage of this approach is that it allows us to link several seemingly unrelated anomalies with a common concept, and it prescribes a very natural experimental test of that concept.

We begin by describing Savage’s approach; in particular, we focus on two of his central postulates on the agent’s preference relation and we explicitly state the properties that these postulates imply on the conditional preference relation that Savage derives from the original one. We then introduce our approach, where the contingent preference relation constitutes a primitive of its own and the sure-thing principle is defined as a consistency restriction between the original and contingent preferences. Finally, we establish the main results connecting the postulates defined over our primitives to Savage’s central postulates.

3.1 Savage’s preference and conditional preference relations

Let $Z$ be a set of consequences and $S$ a set of states. We assume $Z$ and $S$ are finite for simplicity. An act or action $f : S \rightarrow Z$ maps states into consequences, and so $f(s)$ is the consequence of choosing act $f$ if the state of the world is $s$. Let $F$ denote the set of all acts, i.e., all functions from $S$ to $Z$. We assume that the agent is characterized by a preference relation $\succeq \subseteq F \times F$ over the set of acts, and we denote its symmetric and asymmetric parts as $\sim$ and $\succ$, respectively. For an event $A \subseteq S$, we say that $f = g$ in $A$ if $f(s) = g(s)$ for all $s \in A$. We denote the complement of a set $A$ by $A^c$.

The following axiom corresponds to postulate P2 in Savage (1972) and is one of the main (and most controversial) axioms of subjective expected utility theory.

\textsuperscript{7}We focus on the more interesting postulates by designing the experiment in a manner that C-REF holds by design. In particular, in the contingent treatment of the example in Table 2, we do not elicit if subjects are indifferent in event $A^c$, where both acts yield the same payoff, but rather directly tell them that their choice in event $A^c$ will be inconsequential.
Separability (SEP; P2 in Savage). For all $A \subseteq S$ and acts $f, g, f', g' \in F$ such that:

1. In $A^c$, $f = g$ and $f' = g'$.
2. In $A$, $f = f'$ and $g = g'$.
3. $f \succsim g$.

Then $f' \succsim g'$.

SEP is one of the postulates of Savage on which we will focus attention. To illustrate SEP, consider the following example, where $S = \{s_1, s_2, s_3\}$, $A = \{s_1, s_2\}$, $Z = \{0, 1\}$, and the relevant acts are given by:

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<th>$s_1$</th>
<th>$s_2$</th>
<th>$s_3$</th>
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<tbody>
<tr>
<td>$f$</td>
<td>1</td>
<td>0</td>
<td>1</td>
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<tr>
<td>$g$</td>
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<tr>
<td>$f'$</td>
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<td>$g'$</td>
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In particular, SEP says that $f \succsim g$ if and only if $f' \succsim g'$. The Ellsberg and Common-Consequence Allais paradoxes are classic examples where this relationship does not hold and, therefore, SEP is violated.

Savage also defines, for any set $A \subseteq S$, a conditional binary relation “$\succsim$ given $A$” that is derived from the preference relation $\succsim$ as follows:

**Definition 1.** For all $A \subseteq S$ and acts $f, g$, we say that $f \succsim g$ given $A$ if the following condition is satisfied: For any $f', g' \in F$ such that

1. in $A$, $f' = f$ and $g' = g$.
2. in $A^c$, $f' = g'$.

Then $f' \succsim g'$.

As pointed out by Savage, the following properties on the conditional binary relation are straightforward to establish:

**Proposition 1.** (Savage, 1972) If the preference relation $\succsim$ satisfies SEP, then the following statements hold for all $A \subseteq S$:
1. $\succeq$ given $A$ is a preference relation.
2. If $f = g$ in $A$, then $f \sim g$ given $A$.
3. If $f \succeq g$ given $A$ and $f \succeq g$ given $A^c$, then $f \succeq g$. If, in addition, either $f \succ g$ given $A$ or $f \succ g$ given $A^c$, then $f \succ g$.
4. A version of SEP is satisfied for the conditional preference relation (i.e., replace $f \succeq g$ given $A$ and $f' \succeq g'$ given $A$ in SEP above).

The first property is that the conditional binary relation is also a preference relation. The second property says that if two acts give the same consequences on an event, then the acts are regarded as indifferent conditional on the event. The third property is closest to what Savage informally calls the sure-thing principle, which is the motivation he gives for SEP. It roughly says that, if an act is preferred over another act conditional on an event and also conditional on its complement, then that act must also be preferred to the other one according to the original preference relation.\footnote{This property is stated by Savage (1972) in Theorem 2, pg. 24.}

The last property says that the conditional preference relation satisfies a version of the separability condition SEP that is postulated for the original preference relation.

An event $A \subseteq S$ is called null if for all $f, g \in F$, $f \sim g$ given $A$. Savage used his notion of conditional preference to introduce another important axiom, postulate P3:

**P3 (Savage)** For every non-null event $A \subseteq S$ and acts $f, g \in F$ with the property that $f(s) = f(s')$ and $g(s) = g(s')$ for all $s, s' \in S$, $f \succeq g$ if and only if $f \succeq g$ given $A$.

For our purposes, it will be convenient to work with the following postulate.

**Dominance (DOM)** For all $A \subseteq S$ and acts $f, g, f', g' \in F$ such that:
1. $f(s) = f(s')$ and $g(s) = g(s')$ for all $s, s' \in S$.
2. In $A^c$, $f' = g'$.
3. In $A$, $f' = f$ and $g' = g$.
4. $f \succeq g$
   Then $f' \succeq g'$.

DOM is neither weaker nor stronger than P3. It is easy to see that P3 is equivalent to a version of DOM where: (i) DOM is weakened by restricting $A$ to be non-null,
and (ii) DOM is strengthened to require that $f \succeq g$ if and only if $f' \succeq g'$. The reason we use DOM and not P3 in our experimental application is that P3 would require us to assume or test that the relevant event $A$ is non-null.

The next result shows that DOM is actually implied by SEP and P3.

**Proposition 2.** If the preference relation $\succeq$ satisfies SEP and P3, then it also satisfies DOM.

**Proof.** Fix $A \subseteq S$ and acts $f, g, f', g' \in F$ such that: (1) $f(s) = f(s')$ and $g(s) = g(s')$ for all $s, s' \in S$, (2) In $A^c$, $f' = g'$, (3) In $A$, $f' = f$ and $g' = g$, and (4) $f \succeq g$. If $A$ is non-null, then it follows trivially from P3 alone that $f' \succeq g'$. So suppose that $A$ is null. We will use the following result from Savage (Theorem 1(4), pg. 24): If $A$ is null, then $f' \succeq g'$ if and only if $f' \succeq g'$ given $A^c$. Suppose, in order to obtain a contradiction, that is not true that $f' \succeq g'$. Then, by Savage’s Theorem 1(4), it is also not true that $f' \succeq g'$ given $A^c$. In particular, there exist $f'', g'' \in F$ such that (1) in $A^c$, $f'' = f'$ and $g'' = g'$, (2) in $A$, $f'' = g''$, and (3) it is not true that $f'' \succeq g''$. But this must be a contradiction because, by construction, $f'' = g''$. Therefore, $f' \succeq g'$.

DOM is the second postulate implied by Savage’s framework on which we will focus attention. To illustrate DOM, consider the following example, where $S = \{s_1, s_2\}$, $A = \{s_1\}$, $Z = \{x, y, z\}$ are monetary payoffs, and the relevant acts are given by:

<table>
<thead>
<tr>
<th></th>
<th>$s_1$</th>
<th>$s_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$f$</td>
<td>$x$</td>
<td>$x$</td>
</tr>
<tr>
<td>$g$</td>
<td>$y$</td>
<td>$y$</td>
</tr>
<tr>
<td>$f'$</td>
<td>$x$</td>
<td>$z$</td>
</tr>
<tr>
<td>$g'$</td>
<td>$y$</td>
<td>$z$</td>
</tr>
</tbody>
</table>

Suppose that $x \geq y$. It is reasonable for agents to prefer more money to less, so that $f \succeq g$. DOM then implies that $f' \succeq g'$. We will show that this is the kind of dominance relationship that fails in strategic environments, such as auctions and elections. Finally, by taking the space of consequences $Z$ to be a specific set of lotteries, we will show that the common-ratio Allais paradox constitutes a violation of DOM.\(^9\)

\(^9\)When consequences are not monetary payoffs, DOM can be interpreted as requiring utility to be state independent; see, e.g., Gilboa (2009).
Finally, if SEP holds, the following version of DOM, linking both the original and conditional preference relations, is satisfied.

**Proposition 3.** If the preference relation \( \succsim \) satisfies SEP and DOM, the following statement holds: For all \( A \subseteq S \) and acts \( f, g, f', g' \in F \) such that:

1. \( f(s) = f(s') \) and \( g(s) = g(s') \) for all \( s, s' \in S \).
2. In \( A^c \), \( f' = g' \).
3. In \( A \), \( f' = f \) and \( g' = g \).
4. \( f \succsim g \).

Then \( f' \succsim g' \) given \( A \).

*Proof.* Fix \( A \subseteq S \) and \( f, g, f', g' \in F \) satisfying conditions 1-4 in the statement of the proposition. By DOM, it follows that \( f' \succsim g' \). To establish that \( f' \succsim g' \) given \( A \), let \( f'', g'' \in F \) such that (1) in \( A \), \( f'' = f' \) and \( g'' = g' \), (2) in \( A^c \), \( f'' = g'' \). We must show that \( f'' \succsim g'' \). Note that \( f', g', f'', g'' \) are such that (1) In \( A^c \), \( f' = g' \) and \( f'' = g'' \), (2) In \( A \), \( f' = f'' \) and \( g' = g'' \), and (3) \( f' \succsim g' \). It then follows by SEP that \( f'' \succsim g'' \). \( \square \)

The importance of Proposition 3 for our purposes is that it indicates yet another property that is satisfied by the conditional preference relation introduced by Savage.

### 3.2 Contingent preferences

Savage defines the primitive preference relation to be \( \succsim \) and then uses it to derive a conditional preference relation \( \succsim \) given \( A \). In contrast, we adopt an approach where both the original and the conditional preference relations are primitives. The reason is that, in principle, the conditional preference relation constitutes a different conceptual object and it may not be derived from the original one as defined by Savage.

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10If condition 4 in Proposition 3 were replaced by \( f \succsim g \) given \( A \), then the result would also hold (it is simply implied by SEP). But this other property is not the right one for the purpose of our experiments.

11Previous work has already viewed the original and the conditional preference relations as different primitives in the context of sequential decision making, where the decision maker receives information about the realized state. For example, Ghirardato (2002) shows that the Bayesian model of sequential decision making, where the prior is updated according to Bayes’ rule, can be obtained by weakening Savage’s P2, provided that certain consistency conditions are imposed on the relation between the original and conditional preferences. Our theoretical framework follows the spirit of this literature, although we propose a different weakening of Savage’s main axioms that has the Sure-Thing Principle as a central postulate.
We continue to assume that \( \succeq \) is a preference relation and to interpret it as a preference relation over acts before any uncertainty about the state is realized. For clarity, we will often refer to \( \succeq \) as the noncontingent preference relation. But, in contrast to Savage, we also introduce as a new primitive, for all \( A \subseteq S \), a preference relation \( \succeq_A \), with corresponding symmetric and asymmetric parts \( \sim_A \) and \( \succ_A \). We refer to the collection \((\succeq_A)_{A \subseteq S}\) as the contingent preference relation, to distinguish it from Savage’s conditional preference relation, \((\succeq \text{ given } A)_{A \subseteq S}\).\(^{12,13}\)

The interpretation is that \( \succeq_A \) reflects the preferences of the agent over acts when she is asked to commit to an act, conditional on an event \( A \), before any uncertainty about the state is realized. (We focus on static choice but, if we were interested in dynamic choice, there would be yet another preference relation to define that reflects preferences after the agent finds out that event \( A \) is realized; see the discussion in Section 4.2.)

The properties which Savage derived for “\( \succeq \text{ given } A \)” that are listed in Proposition 1 seem very natural. We now state the analog of these properties as potential postulates that our contingent preference relation may satisfy.

**Contingent reflexivity (C-REF)** For all \( A \subseteq S \) and acts \( f, g \in F \): If \( f = g \) in \( A \), then \( f \sim_A g \).

**Sure-thing principle (STP)** For all \( A \subseteq S \) and acts \( f, g \in F \): If \( f \succeq_A g \) and \( f \succeq_{A^c} g \), then \( f \succeq g \). If, in addition, either \( f \succ_A g \) or \( f \succ_{A^c} g \), then \( f \succ g \).

**Contingent separability (C-SEP)** For all \( A \subseteq S \) and acts \( f, g, f', g' \in F \) such that:
1. In \( A^c \), \( f = g \) and \( f' = g' \).
2. In \( A \), \( f = f' \) and \( g = g' \).
3. \( f \succeq_A g \).
Then \( f' \succeq_A g' \).

While we naturally view C-SEP as corresponding to a particular version of SEP in the domain of contingent preferences, it is important to highlight the following

\(^{12}\)While it may be natural to assume that \( \succeq_S = \succeq \), we do not need this assumption for any of our results.

\(^{13}\)Ahn and Ergin (2010) formalize a different kind of framing effect where the primitive is a family of preference relations indexed by partitions, rather than subsets, of the state space. They interpret a partition as a particular description of the contingencies facing the decision maker.
difference: The definition of SEP fixes the noncontingent preference relation $\succeq$ and restricts it to satisfy certain conditions for all subsets $A \subseteq S$. In contrast, in the definition of C-SEP, the preference relation $\succeq_A$ changes as a function of the set $A$.\footnote{In particular, it is not true that C-SEP by itself implies SEP.}

Our first main result is as follows:

**Theorem 1.** If the preference relations $(\succeq_A)_{A \subseteq S}$ and $\succeq_A$ satisfy C-REF, STP, and C-SEP, then $\succeq_A$ satisfies SEP.

**Proof.** Fix $A \subseteq S$ and $f, g, f', g' \in F$ such that (1) In $A^c$, $f = g$ and $f' = g'$, (2) In $A$, $f = f'$ and $g = g'$, and $f \succeq g$. We must establish that $f' \succeq g'$. By C-REF and the fact that $f = g$ in $A^c$, $f \sim_{A^c} g$. Thus, by STP, $f \succeq_A g$ (otherwise, we would have $g \succ f$, a contradiction). Then, by C-SEP, $f' \succeq_A g'$. In addition, C-REF and the fact that $f' = g'$ in $A^c$ implies that $f' \sim_{A^c} g'$. Finally, the facts that $f' \succeq_A g'$ and $f' \sim_{A^c} g'$ imply, by STP, that $f' \succeq g'$, as desired. \hfill \square

Theorem 1 shows that violations of SEP in Savage's setting can be attributed to violations of three different postulates defined over the noncontingent and contingent preference relations.

We now state a fourth postulate on the noncontingent and contingent preference relations, which is the analog of the property stated in Proposition 3 for Savage’s original and conditional preference relations.

**Contingent dominance (C-DOM)** For all $A \subseteq S$ and acts $f, g, f', g' \in F$ such that:

1. $f(s) = f(s')$ and $g(s) = g(s')$ for all $s, s' \in S$.
2. In $A^c$, $f' = g'$.
3. In $A$, $f' = f$ and $g' = g$.
4. $f \succeq g$.

Then $f' \succeq_A g'$.

Our second main result is as follows:

**Theorem 2.** If the preference relations $(\succeq_A)_{A \subseteq S}$ and $\succeq_A$ satisfy C-REF, STP, and C-DOM, then $\succeq_A$ satisfies DOM.
Proof. Let $A \subseteq S$ and let $f, g, f', g' \in F$ be such that: (1) $f(s) = f(s')$ and $g(s) = g(s')$ for all $s, s' \in S$, (2) In $A^c$, $f' = g'$, (3) In $A$, $f' = f$ and $g' = g$, and (4) $f \succsim g$. We want to establish that $f' \succsim g'$. By C-DOM, $f' \succsim_A g'$. By C-REF, $f' \sim_{A^c} g'$. It follows from these two previous statements and STP that $f' \succsim g'$.

Theorem 2 shows that violations of DOM in Savage’s setting can be attributed to violations of three different postulates defined over the noncontingent and contingent preference relations.

Theorems 1 and 2 are the main theoretical results of the paper. As mentioned in the introduction, Savage informally introduced a notion he called the sure-thing principle and used it as motivation for postulates SEP and DOM. By conceptually distinguishing between noncontingent and contingent preferences, we are able to formally define the sure-thing principle, STP. Theorems 1 and 2 describe precisely how this principle underlies both postulates SEP and DOM in Savage’s framework.

These results motivate our subsequent experimental design. In particular, we will look at seemingly unrelated problems where standard postulates in Savage’s framework (SEP and DOM) are shown to fail. We will then document to what extent such failures are related to violations of STP, and whether we also observe failures in either C-SEP or C-DOM. To focus on these questions, we will design the experiment in a way that C-REF will be satisfied by construction. We will find that indeed STP fails in all of these problems, and that there are fewer violations of separability and dominance in contingent versions of these problems.

4 Experimental Design

We study five classic problems in the laboratory: Ellsberg (ELLS), common-consequence Allais (CC ALLAIS), a private-values second-price auction (AUCT), a common-value election (ELECT), and common-ratio Allais (CR ALLAIS). For each of these five problems, we conduct two treatments. In the noncontingent treatment, we study what we called in Section 2 the noncontingent preferences. This is the benchmark treatment and it is intended to replicate existing results in the literature. ELLS and CC ALLAIS constitute examples of violation of separability (SEP), while AUCT, ELECT and CR ALLAIS constitute examples of violation of dominance (DOM).
We also run a second treatment, the \emph{contingent treatment}, where we study what we called in Section 2 the contingent preferences. For each of the five problems, we elicit preferences contingent on the event for which the consequences of the two acts differ, and we investigate if this manipulation has a systematic effect across problems. We design this treatment in a manner that C-REF is satisfied by construction and we evaluate the extent to which the sure-thing principle (STP) and either C-SEP (for \textsc{ells} and \textsc{cc allais}) or C-DOM (for \textsc{auct, elect}, and \textsc{cr allais}) are satisfied. A noteworthy feature of our design is that the subject faces a static choice problem in both the contingent and noncontingent treatments. We discuss the relationship to the dynamic choice literature in Section 4.2.

We conducted both a \emph{between-subjects design}, where each subject participated in one of the problems and in one of the treatments only, and a \emph{within-subjects design}, where each subject participated in both treatments for all of the problems. There are well-known trade-offs between these designs (e.g., Camerer (1995), pg. 633). In particular, the between-subjects design minimizes confounding effects, while the within-subjects design allows us to identify additional primitives such as the correlation between problems. The experiment was conducted at the University of California, Santa Barbara and subjects were recruited using ORSEE (Greiner, 2015). There were a total of 624 participants in the between-subjects design (120, 125, 129, 124, and 126 participants for each of the five problems, respectively) and a total of 131 participants in the within-subjects design. The experiment was conducted using zTree (Fischbacher, 2007).\footnote{A session in the between-subjects (within-subjects) design lasted approximately 30 (90) minutes and on average subjects received $9.50 ($19.10) in compensation.} At the end of the experiment, each subject was asked additional questions to assess her level of risk or ambiguity aversion and cognitive ability. We describe these questions in further detail in the Appendix.

We now describe the two treatments for each of the five problems.

\section*{4.1 Five experimental problems}

\subsection*{4.1.1 Ellsberg problem}

This problem was described in Section 2 and we refer the reader to Table 2 in pg. 8 for reference. Recall that there is a jar with 90 balls. Of the 90 balls, 30 are red and 60 are yellow or blue. A subject must answer two questions, Q1 and Q2, in sequential
order and she does not know the second question when answering the first. For each of the two questions, a ball is randomly drawn (with replacement).

**Noncontingent treatment.** In Q1, the subject must choose between \( f \) and \( g \), while in Q2 the subject must choose between \( f' \) and \( g' \), as described in Table 2. As mentioned earlier, the typical paradox is that a significant number of subjects choose \( g \) in the first question and \( f' \) in the second question. This is a violation of SEP.\(^{16}\) For this treatment and for all other treatments and problems, subjects did not receive feedback until the end of the experiment. Moreover, the written instructions did not include a table such as Table 2 in this example.

**Contingent treatment.** In Q1, we tell the subject that if the drawn ball is blue, the problem ends there and the decision-maker gets $10. But, if the drawn ball is red or yellow, the decision maker has to make a choice between two options: (1) get $10 if the ball is red and (2) get $10 if it is yellow. We then ask the subject to make a choice contingent on the event in which the ball is red or yellow, without yet knowing if this is the event that will happen. Note that a choice between (1) and (2) corresponds to a choice between \( f \) and \( g \) in Table 2. Q2 is identical to the first question except that the decision maker gets $0 if the drawn ball is blue. Thus, the subject is in fact facing a choice between \( f' \) and \( g' \) in Table 2.

**Testable hypotheses.** According to standard theory, there is no difference between the noncontingent and contingent treatments because the subject is essentially facing the same choices over acts in both treatments. In practice, however, one may see a difference. The theoretical framework in Section 3 allows for a difference between the noncontingent preference \( \succcurlyeq \), elicited in the noncontingent treatment, and the contingent preference \( \succcurlyeq_{\{R,Y\}} \), elicited in the contingent treatment. Intuitively, the reason why one may expect different choices in the two treatments is that, in the second treatment, the subject is helped to focus on the event that is payoff relevant for her decision, \{red, yellow\}.

Another important feature of the contingent treatment is that we do not ask for a choice conditional on the event \{blue\}. Rather, we simply tell the subject that her choice does not matter in that event. By doing so, we are essentially guaranteeing that C-REF is satisfied by design in our experiment, so that we can focus attention

\(^{16}\)In accordance with the literature, we take these choices to reflect strict preferences. The underlying assumption is that a subject who is in fact indifferent in both questions chooses the first of the two options with the same probability in each question. The same point holds for all other problems.
on the more interesting postulates, STP and C-SEP. We follow the same idea in the contingent treatments for all other problems: CC ALLAIS, AUCT, ELECT and CR ALLAIS.

Figure 2 (reported earlier in pg. 9) illustrates the testable hypotheses in the context of this problem. A comparison between Q1 and Q2 in the noncontingent treatment is the standard way of testing for SEP in the literature. A comparison between Q1 and Q2 in the contingent treatment provides a test of C-SEP. A comparison between Q1 in the noncontingent treatment and Q1 in the contingent treatment provides a test of STP; the same is true for the comparison between Q2 in both treatments.

4.1.2 Common-consequence Allais problem

There is a jar with 100 balls. Of the 100 balls, 1 is red (R), 10 are yellow (Y), and 89 are blue (B). For each of the two questions, Q1 and Q2, a ball is randomly drawn (with replacement).

Noncontingent treatment. In Q1, the subject must choose between \( f \), which gives $100 million for sure, and \( g \), which gives $500 million if the ball is yellow and $100 million if it is blue.\(^{17}\) In Q2, the subject must choose between \( f' \), which gives $100 million if the ball is red or yellow, and \( g' \), which gives $500 million if the ball is yellow.

<table>
<thead>
<tr>
<th>Question 1</th>
<th>R (1)</th>
<th>Y (10)</th>
<th>B (89)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( f )</td>
<td>$100m</td>
<td>$100m</td>
<td>$100m</td>
</tr>
<tr>
<td>( g )</td>
<td>$0</td>
<td>$500m</td>
<td>$100m</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Question 2</th>
<th>R (1)</th>
<th>Y (10)</th>
<th>B (89)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( f' )</td>
<td>$100m</td>
<td>$100m</td>
<td>$0</td>
</tr>
<tr>
<td>( g' )</td>
<td>$0</td>
<td>$500m</td>
<td>$0</td>
</tr>
</tbody>
</table>

Table 3: Common-consequence Allais problem

Table 3 depicts the choices in each question. The paradox is that a significant number of subjects choose \( f \) (safe option) in Q1 and \( g' \) (risky option) in Q2. This is a violation of SEP.

Contingent treatment. In Q1, we tell the subject that if the drawn ball is blue, the problem ends there and the decision maker gets $100 million. But, if the drawn ball

\(^{17}\)This is the only decision problem for which we use hypothetical payoffs. Huck and Müller (2012) study three alternative ways of implementing the common-consequence Allais problem. They find few violations of SEP with small payoffs, but that violations become more prevalent with hypothetical payoffs expressed in millions of euros.
is red or yellow, the decision maker has to make a choice: (1) get $100 million if the ball is red or yellow and (2) get $500 million if the ball is yellow. We then ask them to make a choice contingent on the event in which the ball is red or yellow, without yet knowing if this is the event that will happen. Note that a choice between (1) and (2) corresponds to a choice between \( f \) and \( g \) in Table 3. Q2 is identical except that the decision maker gets $0 if the drawn ball is blue. Thus, the subject is in fact facing a choice between \( f' \) and \( g' \) in Table 3.

**Testable hypotheses.** This problem has the same structure of ELLS, and so it is straightforward to see that the previous discussion applies here. In particular, Figure 2 (reported earlier in pg. 9) also describes the hypotheses for CC ALLAIS.

### 4.1.3 Auction problem

This problem was described in Section 2 and we refer the reader to Table 1 in pg. 6 for reference. In Section 2, we used the wording of auction theory to describe the problem, but, in the experiment, we used a more neutral language. In particular, we did not make an explicit reference to an auction environment partly due to the concern that subjects may mistakenly interpret it as a first-price auction rather than the less familiar second-price auction.\(^{18}\)

There are three cards, numbered 4.5, 0.5, and 8.5, and one card is randomly drawn. There is only one question in each treatment.

**Noncontingent treatment.** Without knowing the drawn card, the subject must choose an integer between 1 and 8. If the number she chooses is higher than the number on the drawn card, her payoff is $5.5 minus the number on the card (in dollars). If the number she chooses is lower than the number on the card, her payoff is $3. In this problem, one’s choice is only relevant if the card is 4.5, and, in that case, it is optimal to choose 1, 2, 3, or 4.

Table 1 in pg. 6 depicts the problem faced by the agent. As mentioned earlier, we simplify the exposition of the results and codify an optimal choice of 1, 2, 3, or

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\(^{18}\)This is not an issue in second-price auction experiments, where subjects face multiple rounds. While it is typical in experiments of strategic behavior to repeat the same or similar questions many times to test for experience effects, here we decided to only ask each question once, in order to make the results comparable to the standard decision experiments (Ellsberg and Allais). The literature documents that the strategic biases that we replicate here are actually robust to experience (see, for example, Kagel and Levin (1993) for the Auction problem and Esponda and Vespa (2014) for the Election problem).
4 as act \( f' \) and a suboptimal choice of 5, 6, 7, or 8 (overbidding) as act \( g' \). We also define the constant acts \( f \) (payoff of $3 in all states) and \( g \) (payoff of $1 in all states). The paradox in this problem is that a significant fraction of subjects choose \( g' \) over \( f' \). This choice violates DOM under the reasonable assumption that subjects prefer more money to less, i.e., \( f \) is preferred to \( g \).

**Contingent treatment.** We tell the subject that she will get $5 if the drawn card is 0.5, $3 if it is 8.5, and we ask her to make a contingent choice for the event in which the card is 4.5, without her knowing if this is the event that will happen. Thus, the contingent treatment elicits the preference between \( f' \) and \( g' \) according to the contingent preference \( \succeq_{\{4.5\}} \).

**Testable hypotheses.** Figure 1 (reported earlier in pg. 7) describes the hypotheses for AUCT. In the figure, Question 1 corresponds to the question we asked and Question* corresponds to the choice between acts \( f \) and \( g \) in Table 1. Therefore, a comparison between Q1 and Q* in the noncontingent treatment tests DOM. Because Q* seems trivial, we did not ask it; instead, we simply assume that, if Q* were asked, a subject would prefer more to less money, i.e., \( f \) over \( g \). Therefore, DOM is violated in this example provided that a subject prefers \( g' \) to \( f' \) in the noncontingent treatment. Similarly, C-DOM is violated if a subject prefers \( g' \) to \( f' \) in the contingent treatment. Finally, a comparison between Q1 in the noncontingent treatment and Q1 in the contingent treatment tests STP.

**4.1.4 Election problem**

There is a jar with 7 white balls and 3 black balls, and one ball is randomly drawn. There are two computers. If the drawn ball is white (w), both computers vote White (WW). If the drawn ball is black (b), computers vote for different colors (WB). We focus on one question in each treatment, represented in Table 4 as Question 1.

**Noncontingent treatment.** Without observing either the color of the drawn ball or the votes of the computers, the subject must choose between voting for Black and voting for White. If the color chosen by the majority matches the color of the drawn ball, the subject gets $5; otherwise, she gets $0. It is optimal for the subject to vote for Black, since, if her vote matters, it must be that the ball is indeed black.

Table 4 represents the payoffs. Voting for Black is represented by \( f' \) in Table 4 and voting for White is represented by \( g' \). We also define the constant acts \( f \) (a sure payment of $5) and \( g \) (a sure payment of $0) in Table 4, and assume that \( f \) is
Table 4: Election problem. States marked by ◁ have zero probability.

<table>
<thead>
<tr>
<th>Question*</th>
<th>f</th>
<th>$5</th>
<th>wWB</th>
<th>$5</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>g</td>
<td>$0</td>
<td>wWB</td>
<td>$5</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Question 1</th>
<th>f’</th>
<th>$5</th>
<th>$0</th>
<th>$0</th>
<th>$5</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>g’</td>
<td>$0</td>
<td>$5</td>
<td>$0</td>
<td>$5</td>
</tr>
</tbody>
</table>

Table 4: Election problem. States marked by ◁ have zero probability.

preferred to g. The paradox in this problem is that a significant fraction of subjects choose g’ over f’. Whether or not this choice violates DOM depends on the subject’s subjective perception of state wWB. If the subject correctly believes that this state has zero probability, then choosing g’ over f’ violates DOM. Otherwise, all we can say is that an objective version of DOM is violated. It is in principle possible for a subject to subjectively believe that wWB has positive probability and to, therefore, choose g’ over f’ without violating DOM. We will be content with either interpretation (DOM or objective DOM) since our main focus will be on STP.

Contingent treatment. The question is the same, except that we tell subjects that, if both computers vote for the same color, they will receive $5 if the color matches the color of the drawn ball, and $0 otherwise. We then ask them to make a choice contingent on the event that computers vote for different colors, without knowing if this is the event that will happen. This question elicits the subjects’ preference contingent on the pivotal event, i.e., \( \succsim_{\{bWB, wWB\}} \).

Testable hypotheses. Figure 1 (reported earlier in pg. 7) can also be used to describe the hypotheses for elect. In the figure, Question 1 corresponds to the question we asked and Question* corresponds to the choice between acts f and g in Table 4. Therefore, a comparison between Q1 and Q* in the noncontingent treatment tests either DOM or an objective version of DOM, as explained earlier. Because Q* seems trivial, we did not ask it; instead, we simply assume that, if Q* were asked, a subject would prefer more to less money, i.e, \( f \) over \( g \). Therefore, DOM (or its objective version) is violated in this example provided that a subject prefers g’ to f’ in the noncontingent treatment. Similarly, C-DOM (or its objective version) is violated if a subject prefers g’ to f’ in the contingent treatment. Finally, a comparison between Q1 in the noncontingent treatment and Q1 in the contingent treatment tests STP. Note that STP is tested irrespective of whether or not the subject understands
that state $wW B$ has zero probability. For example, a subject may choose $g'$ over $f'$ because she thinks that state $wW B$ is very likely. But the same subject who then prefers $f'$ over $g'$ in the contingent treatment would be violating STP.

### 4.1.5 Common-ratio Allais problem

There is a jar with 100 balls. In each treatment, the subject answers two questions, Q1 and Q2.

**Noncontingent problem.** In Q1, the jar has 12 red, 3 yellow, and 85 blue balls. The subject must choose an option that gives $4 if the drawn ball is red or yellow, and an option that gives $5.30 if it is red. In Q2, the jar has 80 red balls and 20 yellow balls. The subject must choose between an option that gives $4 for sure and an option that gives $5.30 if it is red. Note that the ratio of red to yellow balls is the same in both jars, which explains the term “common-ratio” in this experiment.

To depict this problem in Savage’s framework, let the space of consequences be given by $Z = \{x, y, 0\}$, where $x$ is a lottery that gives a sure payoff of $4, $y$ is a lottery that gives $5.30 with probability .8 and nothing otherwise, and $0$ is a lottery that pays $0 for sure. The set of states is $S = \{RY, B\}$, where $RY$ is the state where the ball drawn from the urn is red or yellow and $B$ is the state where it is blue. Table 5 depicts the choices faced by the subject in each question. In Q1, the subject must choose between $f'$ and $g'$. In Q2, the subject must choose between $f$ (the constant act $x$, i.e., a sure payoff of $4) and $g$ (the constant act $y$, i.e., a lottery that pays $5.30 with probability .8). The typical paradox is that many subjects choose $g'$ in Q1 and $f$ in Q2. This is a violation of DOM.

**Contingent treatment.** In Q1, the question is the same as in the noncontingent treatment, except that if the ball is blue, the decision maker gets $0, and she has to decide what to do in the event that the ball is red or yellow, before knowing if this is the event that will happen. Note that a choice between the options is equivalent to

<table>
<thead>
<tr>
<th>Question 2</th>
<th>$f$</th>
<th>$x$</th>
<th>$x$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$g$</td>
<td>$y$</td>
<td>$y$</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Question 1</th>
<th>$f'$</th>
<th>$x$</th>
<th>$80$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$g'$</td>
<td>$y$</td>
<td>$80$</td>
<td></td>
</tr>
</tbody>
</table>

Table 5: Common-ratio Allais problem
a choice between $f'$ and $g'$ in Table 5. In Q2, the question is identical to Q2 in the noncontingent treatment, and so the choice is between $f$ and $g$ in Table 5.

Testable hypotheses. Figure 1 (reported earlier in pg. 7) also depicts the hypotheses for CR ALLAIS, where, in this particular case, Q2 (which is labelled as Question* in the figure) is the same question for the contingent and noncontingent treatments. A comparison between Q1 and Q2 in the noncontingent treatment tests DOM. This is the standard test in the literature. A comparison between Q1 and Q2 in the contingent treatment tests C-DOM. Finally, a comparison between Q1 in the noncontingent treatment and Q1 in the contingent treatment tests STP.

4.2 Comparison to the dynamic choice literature

A feature of our design that distinguishes our paper from previous work is that we focus on static contexts, in the sense that the subject does not receive any information about the realized state. There is a literature that instead studies decision making in dynamic contexts. This literature defines a conditional preference relation as the preference relation that applies after the agent observes the realization of an event. Two of the main postulates studied in dynamic choice settings include dynamic consistency and consequentialism (e.g., Hammond (1988), Machina (1989), Cubitt (1996)). Dynamic consistency corresponds to comparing our contingent treatment, which elicits a plan of action from the subject, to a sequential treatment in which the agent is informed, before making her choice, that an event has actually occurred. The notion of dynamic consistency is also related to the strategy method in experimental work (e.g., Brandts and Charness, 2011). Under the strategy method, subjects are asked what they would hypothetically do at every contingency. Experiments test if the strategy method introduces a bias by comparing the contingent treatment to a sequential treatment, in which subjects are told the specific contingency that occurred. Consequentialism, on the other hand, corresponds to comparing two sequential treatments where the agent is informed that an event has actually occurred but where the forgone payoffs under the complement of the event are different. In contrast, we focus on the comparison between the noncontingent and contingent treatments, both

---

Because most of the literature implicitly views the noncontingent and contingent treatments as equivalent, some tests of dynamic consistency compare behavior in the noncontingent and sequential treatments. For experiments on dynamic consistency and consequentialism, see Cohen et al. (2000), Dominiak et al. (2012) and Nebout and Dubois (2014).
of which correspond to static choice situations.

5 Results

We divide our results into five main findings. We mainly focus on the results from the treatments in the between-subjects design. We then show that the results are robust to using data from the within-subjects design. Finally, we use the within-subjects design to assess the correlation between decision and game-theoretic problems.

We begin by examining violations of separability and dominance in the noncontingent and contingent treatments.

Finding #1: We replicate the anomalies pointed out in the literature for all noncontingent versions of the problems. In ELLS and CC ALLAIS, the choices of 57.7 and 19.1 percent of subjects, respectively, are inconsistent with SEP. In AUCT, ELECT and CR ALLAIS the choices of 32.3, 84.8 and 49.9 percent of subjects, respectively, are inconsistent with DOM.

Evidence for Finding #1 is presented in columns under the ‘Noncontingent treatments’ heading of Table 6. Consider first the case of ELLS. The table shows that most subjects (50.9%) select $g$ in Q1 and $f'$ in Q2. These choices are consistent with the heuristic of ambiguity aversion (Ellsberg, 1961): subjects in this group prefer $g$ in the first question (where the probability of receiving $10 is known to be 2/3) and $f'$ in the second question (where the probability of receiving $10 is known to be 1/3). There is also a 6.8% of subjects who fail SEP by selecting $f$ in Q1, but $g'$ in Q2. Overall, the proportion of subjects with choices that are inconsistent with SEP is 57.7%. In the case of CC ALLAIS, in line with the literature, we find that the most common violation of SEP occurs when subjects select $f$ in Q1 and $g'$ in Q2. These choices are consistent, for example, with the heuristic of regret aversion (Loomes and Sugden, 1982). Overall, the proportion of subjects with choices that are inconsistent with SEP is 19.1%.

Of all the anomalies we replicated, the one that is hardest to find is the paradox in CC ALLAIS (see, Huck and Müller, 2012 and Blavatskyy et al., 2015). In our experiment, only 19.1% of subjects were inconsistent in the noncontingent treatment, a figure that may seem low but which is consistent with the literature. The proportion of reversals that we find is lower than the average value reported by Huck and Müller (2012) for large hypothetical payoffs, but in line with their findings for highly educated and high income people.
<table>
<thead>
<tr>
<th></th>
<th>Noncontingent treatments</th>
<th></th>
<th>Contingent treatments</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>SEP</td>
<td>DOM</td>
<td>C-SEP</td>
</tr>
<tr>
<td></td>
<td>ELLS</td>
<td>CC ALLAIS</td>
<td>AUCT</td>
</tr>
<tr>
<td>((f, f'))</td>
<td>18.6</td>
<td>22.2</td>
<td>67.7</td>
</tr>
<tr>
<td>((g, g'))</td>
<td>23.7</td>
<td>58.7</td>
<td>0.0</td>
</tr>
<tr>
<td>((f, g'))</td>
<td>6.8</td>
<td>12.7</td>
<td>32.3</td>
</tr>
<tr>
<td>((g, f'))</td>
<td>50.9</td>
<td>6.4</td>
<td>0.0</td>
</tr>
<tr>
<td>% Consistent</td>
<td>42.3</td>
<td>80.9</td>
<td>67.7</td>
</tr>
<tr>
<td>% Reversals</td>
<td>57.7</td>
<td>19.1</td>
<td>32.3</td>
</tr>
<tr>
<td>Participants</td>
<td>59</td>
<td>63</td>
<td>62</td>
</tr>
</tbody>
</table>

Table 6: Proportion of subjects by choices across questions within each treatment (in %)

Notes: 1) In ELLS and CC ALLAIS, \((f, f')\) indicates the proportion of subjects who selected \(f\) in Q1 and \(f'\) in Q2. In AUCT and ELECT, \((f, f')\) indicates choices of \(f\) in Q* and \(f'\) in Q1. We assume that all subjects prefer more money to less and so we impute that all subjects select \(f\) in Q*. In CR ALLAIS, \((f, f')\) indicates choices of \(f\) in Q2 and \(f'\) in Q1.

2) % Consistent presents the addition of subjects who chose \((f, f')\) and subjects who chose \((g, g')\). % Reversals presents the addition of subjects who chose \((f, g')\) and subjects who chose \((g, f')\).
Choices of $g'$ in Q1 of \textsc{auct} and \textsc{elect} are inconsistent with DOM (or objective DOM, in the case of \textsc{elect}) under the assumption that subjects prefer more money to less. In Table 6, we force this assumption by imposing that all subjects would select $f$ in Q*. We find that 32.3% and 84.8% of subjects select $g'$ in \textsc{auct} and \textsc{elect}, respectively. In \textsc{auct}, the observed overbidding is consistent with the illusion that it increases the chance of winning with little cost because the winner pays the second highest bid (Kagel et al., 1987). In \textsc{elect}, the mistake is consistent with the heuristic that subjects choose the color that is more prevalent in the jar.\footnote{The \textsc{elect} problem has received the least amount of attention in the experimental literature, and so to make sure that the conjectured heuristic is correct and to confirm that the labels white or black are not influencing the results, we asked each subject in both treatments a second question. In this other question, the composition of the jar was changed to a majority of black balls (7 black, 3 white). We indeed find that most people vote for Black in this case: 75.8 percent in the noncontingent and 84.1 percent in the contingent treatment (p-value of .24), compared to 15.2 and 54 percent for the first question, respectively.}

Finally, in \textsc{cr allais}, DOM is violated if subjects’ choices are $(f, g')$ or $(g, f')$. Table 6 shows that approximately half of our subjects make choices inconsistent with DOM. As in \textsc{ells} and \textsc{cc allais}, the most prevalent anomaly in \textsc{cr allais} coincides with the one found in the literature, which corresponds to choosing $(f, g')$. These choices are consistent with the certainty effect heuristic (Tversky and Kahneman, 1986).

**Finding #2**: There are fewer anomalies in all contingent versions of the problems relative to the noncontingent versions, except for \textsc{cc allais}. In \textsc{ells} and \textsc{cc allais}, the choices of 27.8 and 28.6 percent of subjects, respectively, are inconsistent with C-SEP. In \textsc{auct}, \textsc{elect} and \textsc{cr allais}, the choices of 12.9, 46.0 and 25.4 percent of subjects, respectively, are inconsistent with C-DOM. Violations of C-SEP or C-DOM correspond to approximately half of the documented violations of SEP and DOM in all problems except in \textsc{cc allais}, where the difference is not statistically significant.

The evidence supporting Finding #2 is presented in the second set of columns of Table 6, under the ‘Contingent treatments’ heading. In all problems we still find some subjects who violate C-SEP or C-DOM, with the proportion of inconsistencies by problem listed in the ‘% of reversals’ row.

We can also contrast violations of DOM and SEP in contingent treatments against violations of C-DOM and C-SEP in noncontingent treatments. Whenever differences across treatments are significant, we find more violations in noncontingent treatments.
Table 7: Testing for STP by comparing between treatments

Notes: The p-values are computed in the following manner. We run a regression where the left-hand side is a variable that takes value 1 if \( f \) (or \( f' \) depending on the question) is selected and the right-hand side variable is a treatment dummy (1=contingent). The reported p-value corresponds to the estimated coefficient for the treatment dummy. For \( \text{ells} \) and \( \text{cc allais} \) we run one regression per question.

Inconsistent choices decrease from 32.3% to 12.9% in \( \text{auct} \) and from 84.8% to 46.0% in \( \text{elect} \), with both differences being statistically significant at the 1% level.\(^{22}\) We also find a decrease in reversals from 57.7% to 27.8% (p-value of .001) in \( \text{ells} \), and from 49.9% to 25.4% (p-value of .004) in \( \text{cr allais} \). Meanwhile, we find no significant difference of reversals in \( \text{cc allais} \). In this case, the proportion of subjects making inconsistent choices actually increases from 19.1% to 28.6%. The difference, however, is not statistically significant (p-value of .213).

We now turn to tests of the sure-thing principle (STP).

**Finding #3:** By comparing the responses for Q1 across treatments, we can reject the hypothesis that STP holds in \( \text{ells} \), \( \text{auct} \), and \( \text{elect} \). By comparing the responses for Q2 across treatments, we can reject the hypothesis that STP holds in \( \text{cc allais} \).

\(^{22}\)We conduct a regression where the right-hand side is a dummy that takes value 1 if \( f' \) is selected and the right-hand side includes a constant and a treatment dummy that takes value 1 if the subject participated in the contingent treatment. The p-values we report correspond to the coefficient estimated for the treatment dummy. A similar approach is followed for the other tests reported in the paper.
Table 7 shows the observed marginal distribution of responses for each problem, question and treatment. The strongest evidence for failure of STP can be obtained by comparing Q1 across treatments. In Q1 of **ells**, **f** is preferred by 25.4% of subjects in the noncontingent treatment and by 52.5% of subjects in the contingent treatment; the difference is statistically significant (p-value of .002). We also find significant differences for Q1 of **elect** (15.2% vs. 54%; p-value of .000) and Q1 of **auct** (67.7% vs. 87.1%; p-value of .010).

For Q1 of **cc allais**, there is a difference but it is marginally not significant (34.9% vs 47.6%; p-value of .15). We do not find a significant difference for Q1 of **cr allais**. Moreover, there is a significant difference for Q2 of **cc allais** (28.6% vs. 50.8%; p-value of .011).

A statistically significant difference between the marginal responses to Q1 or Q2 implies that STP must be violated. This test for STP may not be too informative, however, because the failure to reject differences in Q1 and/or Q2 across treatments does not imply that STP is satisfied. To illustrate, consider the following extreme example: If half of the subjects would hypothetically choose \((f, g')\) in the first treatment and \((g, f')\) in the second treatment and half would choose \((g, f')\) in the first treatment and \((f', g)\) in the second treatment, then we would observe a 50-50 marginal choice in both questions and treatments, when there is in fact 100 percent of subjects violating STP.

A more informative test compares the joint distribution of responses across treatments. If STP holds, then it must be the case that the joint distribution over responses in the noncontingent treatment must equal the joint distribution in the contingent treatment. Of course, the additional informativeness obtained from this test comes at the expense of making the assumption that being faced with Question 1 does not alter responses for Question 2, which is a typical assumption when testing for separability and dominance. While we cannot test this assumption directly in our data, there are two findings that are consistent with this assumption. The first is that our experiment reversed the typical order in which the questions are asked in the **ells** and **cr allais** paradoxes, yet it still finds the same patterns of violations documented in the literature. The second piece of evidence comes from the fact that there are no significant differences for Q2 across treatments of **cr allais** (p-value .45), suggesting that whether a subject faces Q1 in the noncontingent or contingent version does not affect her response for Q2 (recall that Q2 is identical across treatments for **cr allais**).

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Note that for **elect** and **auct**, the test for STP is numerically the same as the test presented in finding #2 to assess the difference between DOM and C-DOM.
Finding #4: By comparing the joint distribution of responses across treatments, we can reject the hypothesis that STP holds in all of the five problems that we study.

Finding #4 is directly implied by Finding #3 for ELLS, CC ALLAIS, AUCT and ELECT. For CR ALLAIS, to establish that the joint distributions are different across treatments, it suffices to show that the proportion of reversals (i.e., choices inconsistent with DOM and C-DOM) are different. We can indeed see from Table 6 that, for CR ALLAIS, the percent of reversals is 49.9 in the noncontingent treatment and 25.4 in the contingent treatment; the difference is statistically significant with a p-value of .004.

Table 8 summarizes our findings from the between-subjects design and also reports new findings from the within-subjects design. The main message that arises is that findings #1 through #4 also hold for the within-subjects design. We now discuss each column of Table 8 in detail.

The first column of Table 8 reports the percent of subjects who fail one of Savage’s postulates under both designs. The only noteworthy difference with the between-subjects design is that a larger percentage of subjects violate SEP in CC ALLAIS (35.1 vs. 19.1), a figure that is in line with the range of findings in the literature. The second column reports the percent who fail the corresponding contingent version of the postulate. Under both designs, violations of C-SEP or C-DOM correspond to approximately half of the documented violations of SEP and DOM in all problems except in CC ALLAIS, where the difference goes in the opposite direction in the between vs. within subjects design, although in both cases the difference is not statistically significant at the 5% level.

The last column of Table 8 reports figures on the percent of subjects who violate STP. In the between-subjects design, subjects only participate in the noncontingent or contingent treatment (but not both), and, therefore, we cannot assess the exact level of violations of STP. Nevertheless, we can compute a tight lower bound for the

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24 For AUCT and ELECT there is a single question, and so the joint distribution is simply the marginal distribution over the single question. Thus, Finding #4 for AUCT and ELECT simply follows from Finding #3. For ELLS and CC ALLAIS, Finding #3 already establishes statistically significant differences in the marginal distributions, which implies that there must be significant differences in the joint distribution.

25 The Online Appendix reports additional results from the within-subjects design.

26 As shown in the Online Appendix, the difference in CC ALLAIS is significant at the 10% level for the within-subjects design.
### Percent of observed violations of SEP or DOM, C-SEP or C-DOM, and STP

<table>
<thead>
<tr>
<th></th>
<th>SEP or DOM</th>
<th>C-SEP or C-DOM</th>
<th>STP</th>
</tr>
</thead>
<tbody>
<tr>
<td>ELLS</td>
<td>between</td>
<td>57.7</td>
<td>27.8</td>
</tr>
<tr>
<td></td>
<td>within</td>
<td>53.4</td>
<td>29.8</td>
</tr>
<tr>
<td>CC ALAIS</td>
<td>between</td>
<td>19.1</td>
<td>28.6</td>
</tr>
<tr>
<td></td>
<td>within</td>
<td>35.1</td>
<td>25.9</td>
</tr>
<tr>
<td>AUCT</td>
<td>between</td>
<td>32.3</td>
<td>12.9</td>
</tr>
<tr>
<td></td>
<td>within</td>
<td>22.9</td>
<td>6.1</td>
</tr>
<tr>
<td>ELECT</td>
<td>between</td>
<td>84.8</td>
<td>46.0</td>
</tr>
<tr>
<td></td>
<td>within</td>
<td>78.5</td>
<td>40.5</td>
</tr>
<tr>
<td>CR ALAIS</td>
<td>between</td>
<td>49.9</td>
<td>25.4</td>
</tr>
<tr>
<td></td>
<td>within</td>
<td>35.1</td>
<td>16.8</td>
</tr>
</tbody>
</table>

Table 8: Failures of STP, SEP or DOM, and C-SEP or C-DOM, by problem.

Notes: Violations of SEP, DOM, C-SEP and C-DOM are computed by contrasting the answers of subjects within the corresponding noncontingent or contingent treatment. We consider STP to be violated if it is violated for one of the questions across the noncontingent and contingent treatments. The between measure of STP violations is a lower bound: it reports the lowest proportion of individual STP violations that is consistent with our data. To emphasize that this measure is a lower bound it is presented in italics.
percent of subjects who violate STP. An advantage of the within-subjects design is that, because subjects participate in both the noncontingent and contingent version of each problem, we can compute the exact percentage of subjects who fail STP. Of course, this figure relies on the assumption that there is no contamination from the fact that a subject participated in both treatments, but the findings reported in the first two columns suggest that this is a reasonable assumption in this context.

Table 8 shows that a large part of the violations in the standard postulates of Savage’s subjective expected utility framework can be attributed to violations in STP in all of the problems that we study. In ELLS and AUCT, the observed lower bound rate of violations of STP reported in the table is higher than the rate of violations of our version of Savage’s postulates for the contingent preferences (C-SEP or C-DOM). In CC ALLAIS, the observed lower bound of STP violations is higher than the rate of violations of SEP. Finally, the observed lower bound of STP violations in ELECT and CR ALLAIS and the rate of C-DOM violations are of comparable magnitude. The figures on the exact percentage of STP violations coming from the within-subjects design are higher than the corresponding violations of C-DOM or C-SEP in all problems, and confirm that STP fails significantly across all problems.

The previous findings indicate that failure of STP is an important force behind violations of the standard postulates, and it provides a unifying explanation of anomalies in a wide range of environments. A question that we now study is whether or not the failure of STP is related across problems. We are able to investigate this question using data from the within-subjects design, since we observe subjects participate in both the noncontingent and contingent treatments in all problems.

Finding #5: There is a significant positive correlation between failures of STP in decision (ELLs, CC ALLAIS, and CR ALLAIS) vs. game-theoretic problems (AUCT and ELECT).

\[27\text{For problems with only one question (AUCT and ELECT), the tight lower bound is } |r_1 - r_2|, \text{ where } r_j \text{ is the proportion that choose the first option in treatment } j. \text{ For the remaining problems, let } p^{NC} = (p^{NC}_{ff}, p^{NC}_{fg}, p^{NC}_{gf}, p^{NC}_{gg}) \text{ denote the proportion of each of the four possible responses, } (f, f'), (f, g'), (g, f'), \text{ and } (g, g') \text{ in the noncontingent treatment, and similarly for } p^{C} \text{ in the contingent treatment. The tight lower bound is } 1 - \min\{p^{NC}_{ff}, p^{C}_{ff}\} + \min\{p^{NC}_{fg}, p^{C}_{fg}\} + \min\{p^{NC}_{gf}, p^{C}_{gf}\} + \min\{p^{NC}_{gg}, p^{C}_{gg}\}. \]

\[28\text{Note that measuring the correlation in the failure of STP is equivalent to measuring the correlation in treatment effect across problems.}\]
We proceed by separating problems into decision problems ($DP$: ELLS, CC ALLAIS, and CR ALLAIS) and game theory problems ($G$: AUCT and ELECT). For each subject and class of problem $k \in \{DP, G\}$, we observe the number of problems for which STP fails, $Y_{DP}$ and $Y_G$, where $Y_{DP} \in \{0, 1, 2, 3\}$ and $Y_G \in \{0, 1, 2\}$. We begin by simply computing the sample correlation coefficient between $Y_{DP}$ and $Y_G$, and obtain a value of 0.29. For a more structured approach, we then estimate a bivariate ordered probit model with the latent, unobserved variables $Y^*_DP$ and $Y^*_G$ affecting the observed variables $Y_{DP}$ and $Y_G$ as follows:

$$Y_{DP} = \begin{cases} 
0 & \text{if } Y^*_{DP} \leq \phi_{1,D} \\
1 & \text{if } \phi_{1,DP} \leq Y^*_{DP} \leq \phi_{2,DP} \\
2 & \text{if } \phi_{2,DP} \leq Y^*_{DP} \leq \phi_{3,DP} \\
3 & \text{if } \phi_{3,DP} \leq Y^*_{DP} 
\end{cases}$$

$$Y_G = \begin{cases} 
0 & \text{if } Y^*_G \leq \phi_{1,G} \\
1 & \text{if } \phi_{1,G} \leq Y^*_G \leq \phi_{2,G} \\
2 & \text{if } \phi_{2,G} \leq Y^*_G 
\end{cases}$$

We assume that

$$Y^*_{DP} = X' \beta_{DP} + \varepsilon_{DP}$$
$$Y^*_G = X' \beta_G + \varepsilon_G,$$

where $X$ includes a constant and the answers that the 131 subjects gave to survey questions, the cognitive reflection test and the risk/ambiguity aversion test at the end of the experiment (see the Appendix for additional details on these observables). We also assume that $(\varepsilon_{DP}, \varepsilon_G)$ are normally distributed with zero mean, unit variance, and correlation coefficient $\rho$. One interpretation of this model is that a subject has a latent level of cognitive ability for decision problems, $Y^*_{DP}$, and another one for game theory problems, $Y^*_G$, that determine her ability or desire to overcome heuristics and satisfy STP. A higher value of the latent variable is associated with a higher number of problems for which the subject satisfies STP. The main parameter of interest, $\rho$, measures the correlation between failures of STP in decision and game-theoretic problems.
We assume that each subject’s observation is drawn from the same distribution and use maximum likelihood to estimate the parameters $\beta_{DP}, \beta_G, \phi_{DP} = (\phi_{1,DP}, \phi_{2,DP}, \phi_{3,DP}), \phi_G = (\phi_{1,G}, \phi_{2,G}),$ and $\rho$.\footnote{For further details see Greene and Hensher (2010).} We present the full results of the estimation in the Online Appendix. Here, we focus on the correlation coefficient. We estimate a correlation coefficient of $\hat{\rho} = 0.34$, with a p-value of 0.001 and a 95\% confidence interval of $[0.1345, 0.5363]$.

6 Conclusion

We document relative large rates of failure of a particular type of hypothetical thinking in classic decision problems and in game-theoretic environments. The particular type of hypothetical thinking underlying these anomalies is what Savage informally called the sure-thing principle (STP) and used as motivation for two of the central postulates in his theory of subjective expected utility. Our approach to formalizing STP is to assume that both the original preference relation and the contingent preference relations are primitives, and we define STP as a particular type of consistency requirement between these primitives. We then establish that violations of some of Savage’s central postulates can be attributed to violations of STP and to violations of contingent versions of these postulates. Our experimental design allows us to evaluate the extent to which standard postulates are violated when controlling for subjects’ difficulty with contingent thinking.

We find that some of the most common anomalies uncovered in laboratory experiments, including overbidding in auctions, naive voting in elections, and Ellsberg and Allais types of paradoxes, spring (at least in large part) from the failure of the type of hypothetical thinking embodied by STP. In particular, many subjects do not reason about hypothetical events the way economic theories typically assume and our findings provide common ground for literatures that have evolved along different paths.

Our strategy is to run subjects through standard versions of each of these canonical problems, which require sophisticated hypothetical thinking on the part of subjects. We then run subjects through slight alterations of each problem, removing the need for them to employ this type of hypothetical sophistication (we call these variations contingent versions of the problem). We find that subjects behave differently in
these two versions of the problem, and that this difference explains about half of the anomalies in many classic problems.

The finding that errors in a set of seemingly dissimilar settings originate from a common source suggests that finding other root phenomena underlying failures of classical assumptions may be an important and fruitful avenue for future research. More narrowly, our results suggest that exploring, both theoretically and empirically, how the models that people construct of their environments might differ from the models built in standard theories may yield critical insight into the source of deviations from these theories.

References


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ton Univ Pr, 2002.


Appendix

Controlling for observables

In this appendix, we show that our treatment effects remain unchanged when we control for observables that we collected at the end of the experiment. We incentivized subjects to provide answers to the Cognitive Reflection Test (CRT, see Frederick, 2005). This test involves three questions (see the Online Appendix) and is intended to measure the extent to which the respondent gives spontaneous (System 1) vs. reasoned (System 2) answers. We also control for other factors that might affect behavior by eliciting additional information for each subject, including a measure of risk aversion (or ambiguity aversion for the Ellsberg problem) and demographic information, including gender, major (economics related or not), and their year of study (freshman, sophomore, junior, senior, or graduate student). The measure of risk or ambiguity aversion is obtained using the bomb risk elicitation test (BRET, see Crosetto and Filippin, 2013).\textsuperscript{30} Table 9 shows descriptive statistics. The measures of risk aversion and cognitive ability are in line with previous literature.\textsuperscript{31}

\begin{table}[h]
\centering
\begin{tabular}{lcccc}
\hline
Variable & Mean & Median & Std. dev. & Observations \\
\hline
Total CRT & 1.45 & 1.00 & 1.11 & 624 \\
BRET (Ambiguity) & 40.45 & 40.00 & 15.50 & 120 \\
BRET (Risk) & 38.64 & 39.50 & 14.97 & 504 \\
Econ Major & 0.204 & - & - & 624 \\
Female & 0.579 & - & - & 624 \\
Junior or older & 0.564 & - & - & 624 \\
\hline
\end{tabular}
\caption{Observables: Summary statistics}
\end{table}

Table 10 shows the results of regressions using data from the between-subjects design, where the right-hand side is a dummy variable that takes value 1 if the subject chooses $f$ (or $f'$ depending on the question). The regression controls for the treatment and the observables described above. As shown by the table, the treatment

\textsuperscript{30}For ambiguity aversion, we modify the experiment by creating ambiguity about the location of the bomb; see the Online Appendix for details.

\textsuperscript{31}Frederick (2005) finds a mean of 1.24 for Total CRT and Crosett o and Filippin (2013) find a mean of 46.5 for BRET (Risk). There is no comparable exercise for ambiguity aversion.
effect highlighted in Finding #3 continues to hold, but the observables are mostly statistically not significant (although the measure or risk or ambiguity aversion tends to have the expected sign, i.e., a lower aversion measure -higher value for the BRET variable- is associated with less risky choice in both of the Allais problems and in Question 2 of the Ellsberg problem.\textsuperscript{32} Table 11 shows the results of regressions of whether or not behavior across Q1 and Q2 is inconsistent for each problem, controlling for the treatment and the observables described above. Once again, the treatment effects reported in Finding #2 continue to hold.

Online Appendix: Additional results for the within-subjects design

Table 12 reproduces the information of Table 6, using answers from the within-subjects design. The data replicate Findings #1 and #2. In particular, in the within-subjects design we also reproduce the anomalies pointed out in the literature for all noncontingent versions of the problems. In ELLS and CC ALLAIS, the choices of 53.4 and 35.1 percent of subjects, respectively, are inconsistent with SEP. In AUCT, ELECT and CR ALLAIS the choices of 22.9, 78.6 and 35.1 percent of subjects, respectively, are inconsistent with DOM.

In the within-subjects design, inconsistent choices decrease from 22.9\% to 6.1\% in AUCT and from 78.6\% to 40.5\% in ELECT, with both differences being statistically significant at the 1\% level. We also find a decrease in reversals from 53.4\% to 29.7\% (p-value of .000 ) in ELLS, and from 35.1\% to 16.8\% (p-value of .001) in CR ALLAIS. In CC ALLAIS, the proportion of subjects making inconsistent choices decreases from 35.1\% to 26.0\%. The difference is significant at the 10\% level (p-value of .057).\textsuperscript{33}

Table 13 reproduces the information of Table 7 using answers in the within-

\textsuperscript{32}Note that in AUCT and ELECT, there is an optimal choice and there is no reason why risk aversion should explain who is sophisticated and makes the right choice.

\textsuperscript{33}We report statistical tests based on a fixed-effects panel regression where the right-hand side is a dummy that takes value 1 if $f'$ is selected and the right-hand side includes a constant and a treatment dummy that takes value 1 for the subject's answer in the contingent treatment and zero for the same subject's answer in the non-contingent treatment. The p-values correspond to the coefficient estimated for the treatment dummy. A similar approach is followed for the other tests reported in the paper. Notice that because the same subject answers both questions, the treatment effects already account for individual-specific differences such as the observables we collect at the end of the session.
<table>
<thead>
<tr>
<th></th>
<th>ELLS</th>
<th>CC ALLAIS</th>
<th>CR ALLAIS</th>
<th>ELECT</th>
<th>AUCT</th>
</tr>
</thead>
<tbody>
<tr>
<td>Q1</td>
<td>-0.116</td>
<td>0.104</td>
<td>0.220***</td>
<td>0.034</td>
<td>0.389***</td>
</tr>
<tr>
<td></td>
<td>(0.086)</td>
<td>(0.090)</td>
<td>(0.087)</td>
<td>(0.088)</td>
<td>(0.076)</td>
</tr>
<tr>
<td>Q2</td>
<td>-0.058</td>
<td>0.015</td>
<td>-0.016</td>
<td>-0.049</td>
<td>0.002</td>
</tr>
<tr>
<td></td>
<td>(0.044)</td>
<td>(0.042)</td>
<td>(0.041)</td>
<td>(0.041)</td>
<td>(0.038)</td>
</tr>
<tr>
<td>Contingent</td>
<td>-0.003</td>
<td>-0.003</td>
<td>-0.001</td>
<td>-0.002</td>
<td>0.003</td>
</tr>
<tr>
<td></td>
<td>(0.003)</td>
<td>(0.003)</td>
<td>(0.003)</td>
<td>(0.003)</td>
<td>(0.003)</td>
</tr>
<tr>
<td>Total CRT</td>
<td>-0.096**</td>
<td>-0.059</td>
<td>-0.059</td>
<td>-0.118</td>
<td>-0.160</td>
</tr>
<tr>
<td></td>
<td>(0.044)</td>
<td>(0.094)</td>
<td>(0.094)</td>
<td>(0.098)</td>
<td>(0.081)</td>
</tr>
<tr>
<td>BRET</td>
<td>-0.003</td>
<td>-0.003</td>
<td>-0.001</td>
<td>-0.002</td>
<td>0.003</td>
</tr>
<tr>
<td></td>
<td>(0.003)</td>
<td>(0.003)</td>
<td>(0.003)</td>
<td>(0.003)</td>
<td>(0.003)</td>
</tr>
<tr>
<td>Econ Major</td>
<td>0.258**</td>
<td>0.030</td>
<td>-0.059</td>
<td>0.040</td>
<td>-0.118</td>
</tr>
<tr>
<td></td>
<td>(0.107)</td>
<td>(0.104)</td>
<td>(0.101)</td>
<td>(0.119)</td>
<td>(0.105)</td>
</tr>
<tr>
<td>Female</td>
<td>-0.121</td>
<td>-0.056</td>
<td>0.095</td>
<td>0.068</td>
<td>-0.113</td>
</tr>
<tr>
<td></td>
<td>(0.091)</td>
<td>(0.094)</td>
<td>(0.094)</td>
<td>(0.098)</td>
<td>(0.081)</td>
</tr>
<tr>
<td>Junior or Older</td>
<td>0.183</td>
<td>-0.106</td>
<td>-0.014</td>
<td>-0.186</td>
<td>-0.292</td>
</tr>
<tr>
<td></td>
<td>(0.103)</td>
<td>(0.107)</td>
<td>(0.091)</td>
<td>(0.088)</td>
<td>(0.081)</td>
</tr>
<tr>
<td>Constant</td>
<td>0.364**</td>
<td>0.933***</td>
<td>0.467***</td>
<td>0.471***</td>
<td>0.857***</td>
</tr>
<tr>
<td></td>
<td>(0.157)</td>
<td>(0.164)</td>
<td>(0.155)</td>
<td>(0.138)</td>
<td>(0.118)</td>
</tr>
</tbody>
</table>

Observations: 120 120 126 126 125 129 124

Table 10: Testing STP - Linear regression results

Note: These regressions use data from the between-subjects design. Left-hand side variable: We run a regression where the left-hand side is a dummy variable that takes value 1 if the subject chooses \( f \) (or \( f' \) depending on the question). Right-hand side variables: Contingent (1=Contingent Treatment), Total CRT (Total number of correct answers in cognitive reflection test), BRET (Box for which subjects stopped the collecting process, a higher number indicates willingness to take more risk/ambiguity), Econ Major (1=Economics/Accounting/Business Economics Majors), Female (1=Subject is a female), Junior or older (1=Subject is a junior, senior or graduate student). Standard errors between parentheses. (*) Significant at 10% level, (**) Significant at 5% level, (***) Significant at 1% level.
<table>
<thead>
<tr>
<th></th>
<th>ELLS</th>
<th>CC ALLAIS</th>
<th>CR ALLAIS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Contingent</td>
<td>-0.297***</td>
<td>0.086</td>
<td>-0.284***</td>
</tr>
<tr>
<td></td>
<td>(0.088)</td>
<td>(0.077)</td>
<td>(0.087)</td>
</tr>
<tr>
<td>Total CRT</td>
<td>0.078*</td>
<td>0.007</td>
<td>-0.010</td>
</tr>
<tr>
<td></td>
<td>(0.046)</td>
<td>(0.036)</td>
<td>(0.040)</td>
</tr>
<tr>
<td>BRET</td>
<td>-0.002</td>
<td>-0.003</td>
<td>0.005</td>
</tr>
<tr>
<td></td>
<td>(0.003)</td>
<td>(0.003)</td>
<td>(0.003)</td>
</tr>
<tr>
<td>Econ Major</td>
<td>-0.110</td>
<td>0.128</td>
<td>-0.223*</td>
</tr>
<tr>
<td></td>
<td>(0.110)</td>
<td>(0.089)</td>
<td>(0.117)</td>
</tr>
<tr>
<td>Female</td>
<td>0.144</td>
<td>0.178**</td>
<td>0.028</td>
</tr>
<tr>
<td></td>
<td>(0.094)</td>
<td>(0.080)</td>
<td>(0.096)</td>
</tr>
<tr>
<td>Junior or Older</td>
<td>0.013</td>
<td>0.033</td>
<td>-0.056</td>
</tr>
<tr>
<td></td>
<td>(0.106)</td>
<td>(0.078)</td>
<td>(0.087)</td>
</tr>
<tr>
<td>Constant</td>
<td>0.650***</td>
<td>0.331**</td>
<td>0.433***</td>
</tr>
<tr>
<td></td>
<td>(0.162)</td>
<td>(0.133)</td>
<td>(0.135)</td>
</tr>
<tr>
<td>Observations</td>
<td>120</td>
<td>126</td>
<td>125</td>
</tr>
</tbody>
</table>

Table 11: Linear regression results for reversals

Note: These regressions use data from the between-subjects design. Left-hand side variable: Dummy that takes value 1 if choice is inconsistent. The choice is inconsistent if the subject selects \((f, g')\) or \((g, f')\). Right-hand side variables: Contingent (1=Contingent Treatment), Total CRT (Total number of correct answers in cognitive reflection test), BRET (Box for which subjects stopped the collecting process, a higher number indicates willingness to take more risk/ambiguity), Econ Major (1=Economics/Accounting/Business Economics Majors), Female (1=Subject is a female), Junior or older (1=Subject is a junior, senior or graduate student). Standard errors between parentheses. (*) Significant at 10% level, (**) Significant at 5% level, (***) Significant at 1% level.
<table>
<thead>
<tr>
<th></th>
<th>Noncontingent treatments</th>
<th></th>
<th>Contingent treatments</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>SEP</td>
<td>DOM</td>
<td>C-SEP</td>
<td>C-DOM</td>
</tr>
<tr>
<td></td>
<td>ELLS CC ALLAIS</td>
<td>AUCT ELECT CR ALLAIS</td>
<td>ELLS CC ALLAIS</td>
<td>AUCT ELECT CR ALLAIS</td>
</tr>
<tr>
<td>((f, f'))</td>
<td>19.9 19.1</td>
<td>77.1 21.4 55.7</td>
<td>35.9 29.7 93.9 59.5 69.5</td>
<td></td>
</tr>
<tr>
<td>((g, g'))</td>
<td>26.7 45.8</td>
<td>0.0 0.0 9.2</td>
<td>34.4 44.3 0.0 0.0 13.7</td>
<td></td>
</tr>
<tr>
<td>((f, g'))</td>
<td>9.9 24.4</td>
<td>22.9 78.6 12.2</td>
<td>13.7 14.5 6.1 40.5 11.5</td>
<td></td>
</tr>
<tr>
<td>((g, f'))</td>
<td>43.5 10.7</td>
<td>0.0 0.0 22.9</td>
<td>16.0 11.5 0.0 0.0 5.3</td>
<td></td>
</tr>
<tr>
<td>% Consistent</td>
<td>46.6 64.9</td>
<td>77.1 21.4 64.9</td>
<td>70.3 74.0 93.9 59.5 83.2</td>
<td></td>
</tr>
<tr>
<td>% Reversals</td>
<td>53.4 35.1</td>
<td>22.9 78.6 35.1</td>
<td>29.7 26.0 6.1 40.5 16.8</td>
<td></td>
</tr>
<tr>
<td>Participants</td>
<td>131 131 131 131 131</td>
<td>131 131 131 131 131</td>
<td>131 131 131 131 131</td>
<td></td>
</tr>
</tbody>
</table>

Table 12: Proportion of subjects by choices across questions within each treatment (in %)

Notes: This table presents data from the within-subjects treatments. 1) In ELLS and CC ALLAIS, \((f, f')\) indicates the proportion of subjects who selected \(f\) in Q1 and \(f'\) in Q2. In AUCT and ELECT, \((f, f')\) indicates choices of \(f\) in Q* and \(f'\) in Q1. We assume that all subjects prefer more money to less and so we impute that all subjects select \(f\) in Q*. In CR ALLAIS, \((f, f')\) indicates choices of \(f\) in Q2 and \(f'\) in Q1. 2) % Consistent presents the addition of subjects who chose \((f, f')\) and subjects who chose \((g, g')\). % Reversals presents the addition of subjects who chose \((f, g')\) and subjects who chose \((g, f')\).
subjects design that allow us to test directly for failures of STP. Consistent with Finding #3 we find that STP fails in all problems. In Q1 of ELLS, \( f \) is preferred by 29.9\% of subjects in the noncontingent treatment and by 49.8\% of subjects in the contingent treatment; the difference is statistically significant (p-value of .001). We also find significant differences for Q1 of ELECT (21.4\% vs. 59.5\%; p-value of .000) and Q1 of AUCT (77.1\% vs. 93.9\%; p-value of .000). For Q1 of CC ALLAIS, the difference is not significant (34.5\% vs 44.3\%; p-value of .854), but there is a significant difference for Q2 (29.8\% vs. 41.2\%; p-value of .025). There are two qualitative differences relative to the results we documented for the between-subjects design. We find a significant difference in Q2 of ELLS (63.4\% vs 51.9\%; p-value 0.050), and we also find significant difference for Q1 of CR ALLAIS (67.9\% vs. 80.9\%; p-value 0.003).

Finally, we provide a comparison across the between-subjects and the within-subjects design. Table 14 provides summary statistics on the observables we collected at the end of the session in the within-subjects design. The statistics are comparable to those of the between-subjects population reported in Table 9 of the Appendix.

Table 13: Testing for STP by comparing between answers to Noncontingent and Contingent problems

<table>
<thead>
<tr>
<th></th>
<th>Noncontingent</th>
<th>Contingent</th>
<th>p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>ELLS</td>
<td>% select ( f ) in Q1</td>
<td>29.8</td>
<td>49.6</td>
</tr>
<tr>
<td></td>
<td>% select ( f' ) in Q2</td>
<td>63.4</td>
<td>51.9</td>
</tr>
<tr>
<td></td>
<td># of Participants</td>
<td>131</td>
<td>131</td>
</tr>
<tr>
<td>CC ALLAIS</td>
<td>% select ( f ) in Q1</td>
<td>43.5</td>
<td>44.3</td>
</tr>
<tr>
<td></td>
<td>% select ( f' ) in Q2</td>
<td>29.8</td>
<td>41.2</td>
</tr>
<tr>
<td></td>
<td># of Participants</td>
<td>131</td>
<td>131</td>
</tr>
<tr>
<td>AUCT</td>
<td>% select ( f' ) in Q1</td>
<td>77.1</td>
<td>93.9</td>
</tr>
<tr>
<td></td>
<td># of Participants</td>
<td>131</td>
<td>131</td>
</tr>
<tr>
<td>ELECT</td>
<td>% select ( f' ) in Q1</td>
<td>21.4</td>
<td>59.5</td>
</tr>
<tr>
<td></td>
<td># of Participants</td>
<td>131</td>
<td>131</td>
</tr>
<tr>
<td>CR ALLAIS</td>
<td>% select ( f' ) in Q1</td>
<td>67.9</td>
<td>80.9</td>
</tr>
<tr>
<td></td>
<td>% select ( f ) in Q2</td>
<td>78.6</td>
<td>74.8</td>
</tr>
<tr>
<td></td>
<td># of Participants</td>
<td>131</td>
<td>131</td>
</tr>
</tbody>
</table>

Notes: The p-values are computed in the following manner. We run a fixed-effects panel regression where the left-hand side is a variable that takes value 1 if \( f \) (or \( f' \) depending on the question) is selected and the right-hand side variable is a treatment dummy (1=contingent). The reported p-value corresponds to the estimated coefficient for the treatment dummy. For ELLS and CC ALLAIS we run one regression per question.
### Table 15: Comparing answers across the between- and within-subjects design

Notes: The p-values are computed in the following manner. We run regression where the left-hand side is a variable that takes value 1 if $f$ (or $f'$ depending on the question) is selected and the right-hand side variable is a treatment dummy (1=subject participated in the between-subjects design). The reported p-value corresponds to the estimated coefficient for the design dummy. For ELLS and CC ALLAIS and CR ALLAIS we run one regression per question.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Mean</th>
<th>Median</th>
<th>Std. dev.</th>
<th>Observations</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total CRT</td>
<td>1.44</td>
<td>1.00</td>
<td>1.20</td>
<td>131</td>
</tr>
<tr>
<td>BRET (Risk)</td>
<td>43.42</td>
<td>44.00</td>
<td>16.40</td>
<td>131</td>
</tr>
<tr>
<td>Econ Major</td>
<td>0.191</td>
<td>-</td>
<td>-</td>
<td>131</td>
</tr>
<tr>
<td>Female</td>
<td>0.603</td>
<td>-</td>
<td>-</td>
<td>131</td>
</tr>
<tr>
<td>Junior or older</td>
<td>0.466</td>
<td>-</td>
<td>-</td>
<td>131</td>
</tr>
</tbody>
</table>

Table 14: Observables: Summary statistics (within-subjects design)

Table 15 compares answers in the between- and within-subjects design question by question. We find no statistical difference in the comparison question by question with one exception. In the case of the contingent CR ALLAIS treatment, we find that more subjects select $f'$ in question 1 of the the within-subjects design relative to the between-subjects design.